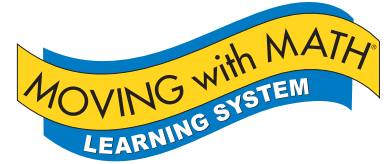


# *Moving with Math*<sup>®</sup> for: Utah's Response to Intervention



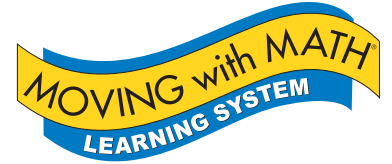
Math Teachers Press, Inc.



## **The MOVING WITH MATH Difference Meeting the Needs of Response to Intervention**

- I. The Problem**
- II. The Solution**
  - Moving with Math Learning System*
    - a. Assessment**
    - b. Instruction**
- III. Meeting Your Needs for RTI**
- IV. Strategies and Results**
- V. Recommendations**
- VI. Conclusion**

# The Problem

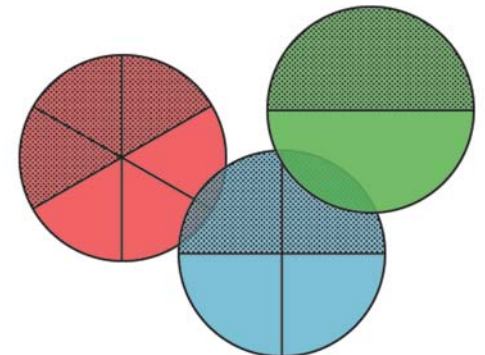


**National Results  
Show Students Lack  
Conceptual  
Understanding**

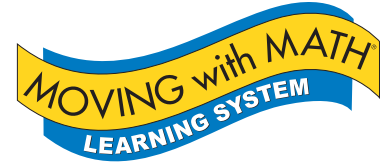
## 4th Grade Results

Concept 3: Fractions	% Answering Correctly
How many fourths make a whole? Answer _____	50 %

National Assessment of Educational Progress



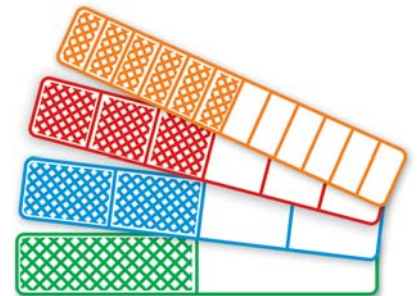
# The Problem



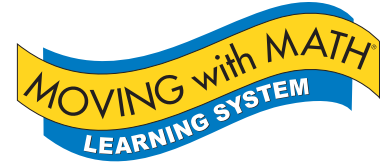
**National Results  
Show Students Lack  
Conceptual  
Understanding**

Problem (13 year-olds)	% Answering Correctly
$\frac{1}{2} + \frac{1}{3}$	33%
$\frac{3}{4} + \frac{1}{2}$	33%
Estimate the best answer for $\frac{12}{13} + \frac{7}{8}$ <b>A 1      B 2      C 19      D 21</b>	25%

National Assessment of Educational Progress



# The Problem



## Disaggregated Group Results

Results Reveal a Divide in Math Classrooms Between the Students Who “Get Math” and the Students Who Don’t

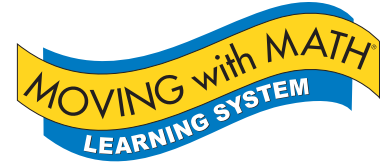
Problem	Average	Upper Quartile	Lower Quartile
$\begin{array}{r} 47 \\ - 18 \\ \hline \end{array}$	60%	90%	20%

MATHEMATICS DEPARTMENT - MINNEAPOLIS PUBLIC SCHOOLS  
Second Grade Math Benchmark Test Results

Problem	Average	Upper Quartile	Lower Quartile
$\begin{array}{r} 34 \\ \times 2 \\ \hline \end{array}$	83%	99%	68%

MATHEMATICS DEPARTMENT - MINNEAPOLIS PUBLIC SCHOOLS  
Fourth Grade Math Benchmark Test Results

# The Problem



## Disaggregated Group Results

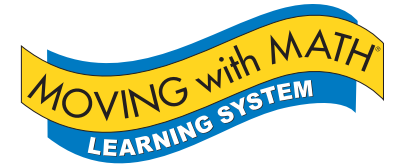
Results Reveal a Divide in Math Classrooms Between the Students Who “Get Math” and the Students Who Don’t



\*A difference of 20% or greater is statistically significant.

# The Solution

## The *Moving with Math*<sup>®</sup> Difference

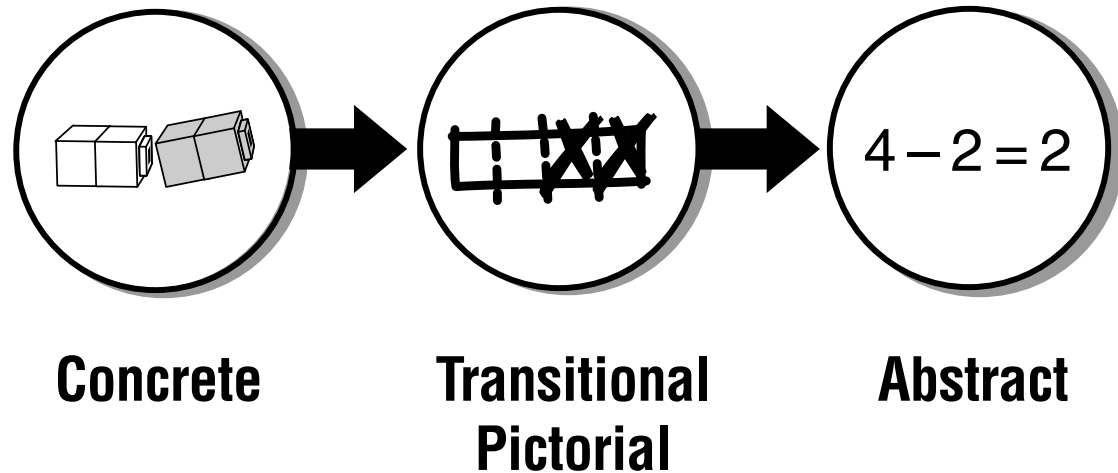
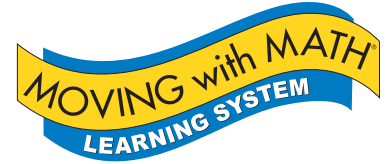


- Curriculum alignment
- Conceptually based instruction
- Research-based strategies with proven results



# The Solution

## The Three Stages of Learning

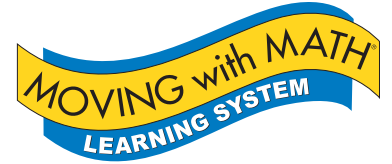


**“All students benefit from a Concrete–Representational–Abstract (CRA) teaching sequence that introduces concretely, moves to visual and pictorial representations, and culminates in abstract symbolic reasoning and representation.”**

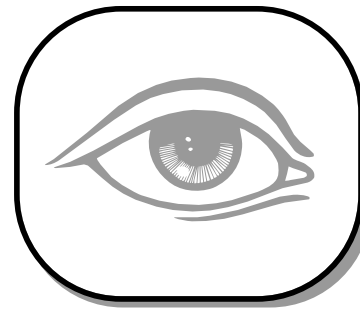


# The Solution

## The Three Learning Styles



**Kinesthetic**



**Visual**



**Auditory**

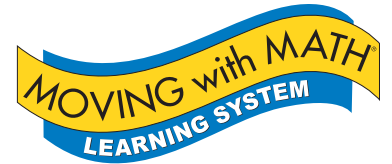
**“Allowing students differentiated ways of accessing and expressing mathematics increases engagement and successful acquisition of concepts and skills.”**

*-Utah’s 3-Tier Model of Mathematics Instruction, Page 19*

# Moving with Math<sup>®</sup> Learning System

## Curriculum Alignment

A system of assessment and instruction where everything is tied to objectives and standards..with proven results!



# Moving with Math<sup>®</sup> Learning System

## Step 1: Correlations to Objectives and Common Core State Standards



### B1 Correlation to Objectives

Use this table to match objectives to pages in the Lesson Plans, Student Book and *Skill Builders*.

Obj.	Objective Description	Lesson Plan/ Student Book Pages	Skill Builders
B-1	Identify place values in numbers up to 3 digits, including expanded notation and use of calculators.	2-4, 66	1-1, 1-2, 1-3, 1-4
B-2	Compare and order numbers up to 6 digits, using models and a number line.	5-6, 16, 19	2-1, 2-2, 2-3, 2-4
B-3	Recognize and extend patterns using multiples of 1 to 10, 100, and 1000, with objects and symbols.	8-11, 14	3-1, 3-2
B-4	Write 4- to 6-digit numbers from words or models.	15, 21	4-1, 4-2, 4-3
B-5	Write words for any numeral up to 6 (or 9) digits.	20	5-1, 5-2
B-6	Identify place values in a 4- to 6-digit number.	17-18	6-1, 6-2, 6-3, 6-4, 6-5
B-7	Round a 2- to 4-digit number to nearest 10 using models, a number line, and patterns.	22-23	7-1, 7-2
B-8	Round a 3- to 4-digit number to nearest 100.	24-26	8-1, 8-2, 8-3
B-9	Determine from commutative or associative property a missing number in an addition equation. Write and solve mathematical expressions with parentheses.	27-28	9-1, 9-2
B-10	Add up to 3-digit numbers with 0 to 2 regroupings. Use a five-step plan to solve addition word problems.	33-38, 60, 67	10-1 to 10-16
B-11	Add 3 or 4 numbers up to 3 digits with regrouping.	39-40	11-1, 11-2
B-12	Add 4- to 6-digit numbers with regrouping.	71-72	12-1, 12-2
B-13	Manipulate and solve addition equations of varying lengths in vertical and horizontal formats.	73, 77	13-1
B-14	Recognize "sum" and the plus sign. Explore mathematical expressions using variables.	29-32, 38	14-1, 14-2, 14-3, 14-4
B-15	Subtract up to 3-digit numbers with 0 to 2 regroupings. Use a five-step plan to solve 1- and 2-step problems.	45-48, 50-55, 61, 63-65	15-1 to 15-19
B-16	Subtract 3-digit numbers with regroupings across 0.	56	16-1, 16-2
B-17	Subtract 4- or 5-digit numbers with regroupings.	74-75	17-1, 17-2
B-18	Manipulate and solve subtraction equations of varying lengths in vertical and horizontal formats.	76	18-1
B-19	Recognize "difference" and the minus sign. Relate subtraction to addition. Explore mathematical expressions using variables.	41-44, 49	19-1 to 19-7
B-47	Explore the concept of decimals. Perform basic operations with decimals and money amounts.	57-59, 62	47-1, 47-2, 47-3, 47-4
B-48	Graph points and identify coordinates for points on a coordinate grid.	12, 13	48-1, 48-2, 48-3
B-50	Plan, organize, display and interpret data using various graphical forms. Find the range, median, mode, and mean.	68-70	50-1, 50-2, 50-3, 50-4

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## Step 2: Assess with Pre-Test



Name \_\_\_\_\_

Score \_\_\_\_\_  
(50 possible)

### Number Sense, Addition, Subtraction Pre-Test

1. Which digit is in the hundreds place?

6 5 3

(Obj. 1)

- A 6  
B 0  
C 5  
D 3

2. Which number is the standard numeral for  $300 + 20 + 7$ ?

- A 300,207  
B 40,609  
C 3027  
D 327

(Obj. 1)

3. Which number is the greatest?

- A 5412  
B 6421  
C 6412  
D 5642

(Obj. 2)

4. This graph shows the pounds of recycling by grade.

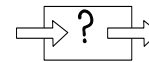
Grade	Pounds of Recycling
2	648
3	571
4	598
5	652

Which grade collected the most cans for recycling?

- A Grade 2  
B Grade 3  
C Grade 4  
D Grade 5

(Obj. 2)

5. A number machine makes numbers in a pattern. What number will come next?

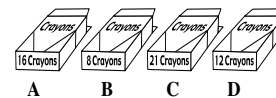


3, 6, 9, \_\_\_\_\_

- A 10  
B 11  
C 12  
D 13

(Obj. 3)

6. An even number of crayons is to be packed in each box. Which box is not packed correctly?



(Obj. 3)

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## Step 3: Interpret Results with Student Progress Report

Helpful tool for IEPs!



### B1 Student Progress Report

Name \_\_\_\_\_

Record results from the Pre- and Post-Test here to see strengths and weaknesses on test questions aligned to the objectives for this level.

Test Item	Pre-Test	Post-Test	Objective # and Description	Test Item	Pre-Test	Post-Test	Objective # and Description
1.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-1</b> Identify place values in numbers up to 3 digits.	29.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-15</b> Subtract up to 3-digit numbers. Employ a five-step plan to solve one- and two-step word problems.
2.	<input type="checkbox"/>	<input type="checkbox"/>		30.	<input type="checkbox"/>	<input type="checkbox"/>	
3.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-2</b> Compare and order numbers up to 6 digits.	31.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-16</b> Subtract 3-digit numbers and money with regroupings across zero.
4.	<input type="checkbox"/>	<input type="checkbox"/>		32.	<input type="checkbox"/>	<input type="checkbox"/>	
5.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-3</b> Recognize, describe and extend patterns. Identify patterns for odd and even numbers.	33.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-17</b> Subtract 4- or 5-digit numbers with regroupings.
6.	<input type="checkbox"/>	<input type="checkbox"/>		34.	<input type="checkbox"/>	<input type="checkbox"/>	
7.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-4</b> Write a 4-, 5- or 6-digit numeral from printed words or models.	35.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-18</b> Manipulate and solve subtraction equations of varying lengths in vertical and horizontal formats.
8.	<input type="checkbox"/>	<input type="checkbox"/>		36.	<input type="checkbox"/>	<input type="checkbox"/>	
9.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-5</b> Write the words for any numeral up to 6 (or 9) digits.	37.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-19</b> Recognize subtraction vocabulary, including "difference" and the "-" sign. Explore mathematical expressions and open number sentences that use variables.
10.	<input type="checkbox"/>	<input type="checkbox"/>		38.	<input type="checkbox"/>	<input type="checkbox"/>	
11.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-6</b> Identify place values in a 4, 5- or 6-digit number.	39.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-47</b> Explore the concept of decimals, and solve problems with decimals and money. Round money to the nearest dollar or nearest 10 cents.
12.	<input type="checkbox"/>	<input type="checkbox"/>		40.	<input type="checkbox"/>	<input type="checkbox"/>	
13.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-7</b> Round a 2-, 3- or 4-digit number to the nearest ten.	41.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-48</b> Graph points and identify coordinates of points shown on a coordinate grid.
14.	<input type="checkbox"/>	<input type="checkbox"/>		42.	<input type="checkbox"/>	<input type="checkbox"/>	
15.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-8</b> Round a 3- or 4-digit number to the nearest hundred.	43.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-10</b> Add up to 3-digit numbers. Employ a five-step plan to solve word problems involving addition.
16.	<input type="checkbox"/>	<input type="checkbox"/>		44.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-15</b> Subtract up to 3-digit numbers. Employ a five-step plan to solve one- and two-step word problems.
17.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-9</b> Determine from the commutative (order) or associative (grouping) property a missing number in an addition equation.	45.	<input type="checkbox"/>	<input type="checkbox"/>	
18.	<input type="checkbox"/>	<input type="checkbox"/>		46.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-50</b> Plan, organize, display and interpret data in various graphical forms.
19.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-10</b> Add up to 3-digit numbers. Employ a five-step plan to solve word problems involving addition.	47.	<input type="checkbox"/>	<input type="checkbox"/>	
20.	<input type="checkbox"/>	<input type="checkbox"/>		48.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-47</b> Explore the concept of decimals, and solve problems with decimals and money. Round money to the nearest dollar or nearest 10 cents.
21.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-11</b> Add three or four 2- or 3-digit numbers with regrouping.	49.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-50</b> Plan, organize, display and interpret data in various graphical forms.
22.	<input type="checkbox"/>	<input type="checkbox"/>		50.	<input type="checkbox"/>	<input type="checkbox"/>	
23.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-12</b> Add 4- to 6-digit numbers with regrouping.				
24.	<input type="checkbox"/>	<input type="checkbox"/>					
25.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-13</b> Manipulate and solve addition equations of varying lengths in vertical and horizontal formats.				
26.	<input type="checkbox"/>	<input type="checkbox"/>					
27.	<input type="checkbox"/>	<input type="checkbox"/>	<b>B-14</b> Recognize addition vocabulary, including "sum" and the "+" sign. Explore mathematical expressions and open number sentences that use variables.				
28.	<input type="checkbox"/>	<input type="checkbox"/>					

Total Correct (out of 40 items)



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## Step 4: Connect to Home



### Family Math Letter

Dear Parent:

Your child is enrolled in a class to strengthen understanding and achievement in math. The class will learn place value up to 6 digits. They will add and subtract large numbers with and without regrouping. They will also be solving word problems that are relevant to everyday life and subjects in school.

Solving word problems is a difficult skill. To help your child at home, tell stories involving addition and subtraction. Using counters and models and understand the action in the problems.

The class will include a Pre-Test, a Post-Test, regular re-assessments, and activities provided with a list of your child's strengths and weaknesses activities and games at home.

It is important that you be involved in your child's education here, and I hope that you will contact me with any questions or hearing from you.

Return the completed Family Math pages to receive a copy of your child's report.

Sincerely,

Phone: \_\_\_\_\_

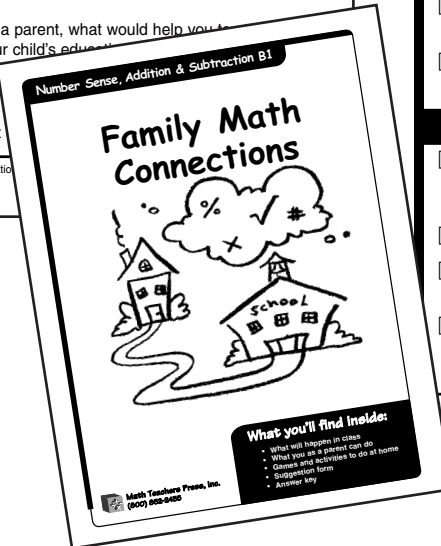
School Website: \_\_\_\_\_

### Parent Feedback

- How could this session be improved? Circle all that apply.  
 A. More practice pages in this booklet B. More data  
 C. Additional opportunities to communicate with the teacher  
 D. My child's progress E. Other \_\_\_\_\_
- What did your child enjoy most about this class?  
 \_\_\_\_\_
- What was most difficult for your child to learn?  
 \_\_\_\_\_
- As a parent, what would help you to support your child's education?  
 \_\_\_\_\_

Parent \_\_\_\_\_

B1 Foundations



## Student Strengths and Weaknesses

### What this report shows:

The essential math skills listed here are necessary for your child's future math success. This report shows the skills your child already knows (marked with a ✓) as well as those your child still needs to learn during this course (marked with an ✗). At the end of this class, your child will be tested again on these same skills.

#### Numeration

- Identify place values in numbers up to 3 digits.
- Compare and order numbers up to 6 digits.
- Recognize, describe and extend patterns. Identify patterns for odd and even numbers.
- Write a 4-, 5- or 6-digit numeral from printed words or models.
- Write the words for any numeral up to 6 (or 9) digits.
- Identify place values in a 4, 5- or 6-digit number.
- Round a 2-, 3- or 4-digit number to the nearest ten.
- Round a 3- or 4-digit number to the nearest hundred.

#### Addition

- Determine from the order or grouping property a missing number in an addition equation.
- Add up to 3-digit numbers.
- Add three or four 2- or 3-digit numbers with regrouping.
- Add 4- to 6-digit numbers with regrouping.

#### Subtraction

- Manipulate and solve addition equations of varying lengths in vertical and horizontal formats.
- Recognize addition vocabulary, including "sum" and the "+" sign.
- Subtract 3-digit numbers. Solve word problems using subtraction.
- Subtract 3-digit numbers and money with regroupings across zero.
- Subtract 4- or 5-digit numbers.
- Solve subtraction equations of varying lengths.
- Recognize subtraction vocabulary, including "difference" and the "-" sign.

#### Decimals

- Solve problems with decimals and money amounts. Make change for a \$5 bill.

#### Coordinate Graphing

- Graph points and identify coordinates of points shown on a coordinate grid.

#### Data Analysis

- Plan, organize, display and interpret data as bar graphs.

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## Step 5: Teach

Pacing Calendars provide instructional support.



Lessons 1–5		30-Lesson Pacing Calendar				Foundations B1
	Lesson 1	Lesson 2	Lesson 3	Lesson 4	Lesson 5	
<b>Daily Review</b> ‡	Daily Review 1	Daily Review 2	Daily Review 3	Daily Review 4	Check Point 5 and 6— may be used as a quiz	
<b>Lesson Plan*</b> <b>Hands-on Math Activities</b>	<b>Objective:</b> To explore and name base ten blocks, and develop an understanding of place values. To build models and draw pictures of numerals. To write numbers in expanded notation.  <b>Materials:</b> Masters 1, 2, 20 and 21, base ten blocks, 6-sided dice.  <b>Lesson Plans:</b> pp. 2–4 <b>Student Book:</b> pp. 2–4	<b>Assessment Pre-Test</b>  <b>Assessment:</b> Administer Pre-Test to evaluate students' grasp of math skills considered essential for future math success.  The Pre-Test is in the Assessment section of the Teacher Manual.	<b>Objective:</b> To compare and order 2- and 3-digit numbers. To estimate the number of objects in a jar.  <b>Materials:</b> Masters 3 and 4, base ten blocks, index cards, 6-sided dice, playing cards, clear jar, 100 marbles, 100 pennies, large gumballs or golf balls  <b>Lesson Plans:</b> pp. 5–7 <b>Student Book:</b> pp. 5–7	<b>Objective:</b> To discover patterns for odd and even numbers. To skip count by 3, 4, 5, and 6. To find the pattern in an arithmetic sequence.  <b>Materials:</b> Masters 5, 6 and 7, one-inch squares, overhead squares, counters or cubes  <b>Lesson Plans:</b> pp. 8–10 <b>Student Book:</b> pp. 8–10	<b>Objective:</b> To introduce function machines. To locate points on a coordinate grid.  <b>Materials:</b> Masters 3 and 5, empty milk carton, large box, index cards, interlocking cubes, masking tape, crayons  <b>Lesson Plans:</b> pp. 11–13 <b>Student Book:</b> pp. 11–13	Lesson Content
<b>Skill Builders</b>	Skill Builders: 1-1, 1-2, 1-3, 1-4		Skill Builders: 2-1, 2-2	Skill Builders: 3-1, 3-2, 42-1	Skill Builders: 14-3, 14-4, 48-3	
<b>Read-to-Me</b>	<i>One Hundred Is a Family</i> , p. 2 <i>101 Dalmatians...</i> , p. 3 <i>Amazing &amp; Incredible Counting Stories</i> , p. 4		<i>Just Enough Carrots</i> , p. 5 <i>Gulliver's Travels</i> , p. 5 <i>One, Two, Three, Sassafras!</i> p. 6 <i>Betchal</i> , p. 7	<i>Two Ways to Count to Ten</i> , etc., p. 8 <i>Spunky Monkeys on Parade</i> , etc., p. 9	<i>Roll Over! A Counting Song</i> , p. 11 <i>A Fly on the Ceiling</i> , p. 13	
<b>Math Games</b>	Hammer to 100 Game, p. 4 Chisel to 0 Game, p. 4		Who Has More? p. 6 Smallest, Middle or Greatest, p. 6 How Many Ways? p. 6 Estimation Contest, p. 7	Buzz Game, p. 9	What's My Rule? p. 11	
<b>Journal Prompt</b>	Journal Prompt: Student Book p. 4			Journal Prompt: Student Book p. 9		
<b>Test Prep</b>				Test Prep: Student Book p. 8	Test Prep: Student Book p. 11	Assessment
<b>Sum it Up!</b>	Sum it Up! Student Book p. 3		Sum it Up! Student Book pp. 5, 7			
<b>Family Math</b> §		<b>Family Math:</b> Send home Family Math Letter and Student Strengths and Weaknesses Report, pp. 2–3				Home

Pacing Calendar

xiii

‡ Daily Reviews and Check Points are found on pages 81–96 of the **Student Book** and copies are in the Assessment section of the **Teacher Manual**.

\* All page numbers, unless otherwise indicated, refer to the **Lesson Plans/Student Book**.  
§ Make copies from the Family Math section of the **Teacher Manual**.

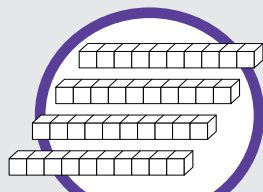


# Moving with Math<sup>®</sup> Learning System

## Step 5: Teach



Manipulatives



Pictures

Hundreds	Tens	Ones
1	7	6

Symbols



### Objective:

To explore and name base ten blocks. To match the blocks with their place value names.

### Materials:

Base ten blocks, Place Value Mats (Masters 1 and 2)

*Note: Before class, make copies of Master 20 (Vocabulary Cards). Make copies of Master 21 (My Math Glossary) and distribute to each student.*

### Vocabulary:

different, place value names, same



*One Hundred Is a Family*, Ryan, Pam Munoz (Activity 2)

## Concrete Stage

### Introducing Base Ten Blocks

The main reason students make errors with whole number algorithms is that they do not understand multi-digit numeration. They do not know that 43 means 4 tens and 3 ones or  $40 + 3$ .

Base ten blocks are ideal for teaching numeration concepts because students can see the abstract concept of place value each time they pick up a block. One tens block is always seen both as 1 ten and 10 ones.

Each pair or small group should have 20 ones blocks, 10 tens blocks, 10 hundreds blocks, and a place value mat.

Explain the benefits and proper use of manipulatives. Set ground rules for using them and discuss take-out and clean-up routines.

**We are going to begin using base ten blocks. See what you can discover about your blocks.** Allow exploratory time. Students might make buildings, roads and parking ramps.

Encourage students to look for patterns. **We can find important patterns if we ask ourselves how these blocks are the same, or alike, and how they are different, or not alike.**

Write 2 columns on the board:

How are the blocks the same?

How are the blocks different?

**What is one way the blocks are the same?** (e.g., same material) After a period of time, ask students to share.

Same	Different
made of wood	sizes
natural color	shapes
points & corners	volumes
solids	weight
made of 1 cm cubes	
10 of 1 block = 1 of the next larger block	

## Representational Stage

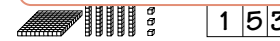
### Three-Digit Place Value

Walter O'Reilly scored a total of 122 NHL playoff goals in his career.

We can show this number with Base Ten Blocks.



## Abstract Stage



one hundred five three  
 one hundred fifty-three



one hundred seventy-six  
 one hundred seven six



one hundred ninety  
 one hundred nine

**How many different sizes do you have? (3) Put 1 of each size in front of you. We call the smallest block the "ones" or "units" block. How many ones does it take to make the next-sized block? (10) We name this block the "tens" or "long" block.**

**How many of the ones blocks are the same as the largest block? (100) We name this block the "hundreds" or "flat" block.**

**The words "ones," "tens," and "hundreds" are place value names.**

Display 1 hundred, 2 tens, 5 ones. Place the blocks correctly on a Place Value Mat. Then say the words for the blocks, **one hundred twenty-five**.

### About This Page

Work through the example together. **Look at problem 1. What blocks are shown?** (1 hundred, 5 tens, 3 ones) **Write the number in the correct place on the chart.** (153)

**To say this number aloud, touch the biggest block and say its value.** (100) **Now touch the next biggest blocks and say their value.** (50) **Then touch the smallest blocks and say their value.** (3) **Now say the number together as you touch the blocks.** (one hundred fifty-three)

Have students complete problems 2 and 3 on their own or with a partner.

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## Step 5: Teach

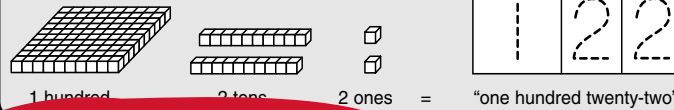
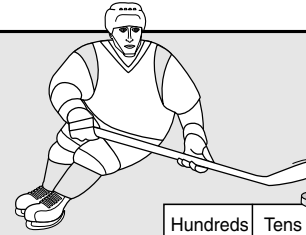
Pictures of manipulatives on the student page help transition to the abstract.



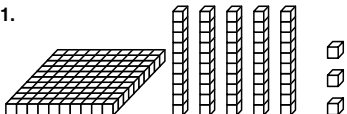
### Three-Digit Place Value

Wayne Gretzky scored a total of 122 NHL playoff goals in his career.

We can show this number with base ten blocks.

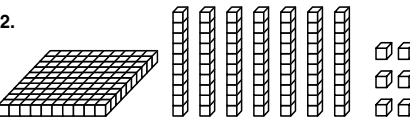


Write the number. Shade the bubble next to the correct name.

1. 

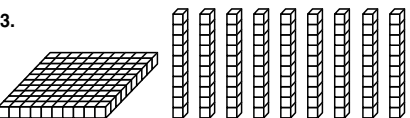
Hundreds	Tens	Ones

- one hundred five three  
 one hundred fifty-three

2. 

Hundreds	Tens	Ones

- one hundred seventy-six  
 one hundred seven six

3. 

Hundreds	Tens	Ones

- one hundred ninety  
 one hundred nine

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## Step 5: Teach

Curricular  
embedded  
assessments



## Sum It Up!



What important pattern with base ten blocks helps us understand place value?

## Journal Prompt



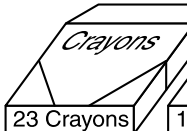
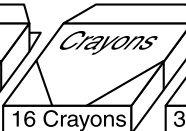
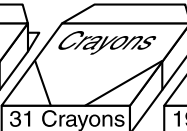
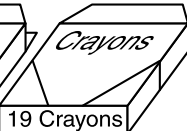
What number is missing in the pattern? Use words, numbers and pictures to tell how you know.

20, 24, \_\_\_\_\_, 32, 36

## Test Prep

TEST PREP 

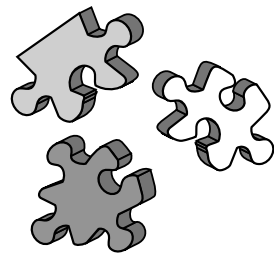
Maren packed an even number of crayons into her box. Which box did Maren pack?

				(A)
<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	(B)
				(C)
				(D)

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## Step 5: Teach

Games motivate and engage students.



### *Hammer to 100 Game*

Game for 2 players. Use base ten blocks in a pile: 1 hundred flat, 20 tens and 30 ones. Each player takes turns tossing a 6-sided die and removing the number tossed from the pile. Each time a player gets 10 ones, they are exchanged for 1 ten. The first player to get exactly 10 tens on a toss exchanges it for the 100 flat and is the winner.

# Moving with Math<sup>®</sup> Learning System

## Step 6: Review and Reteach

Daily Reviews and Weekly CheckPoints are correlated to learning objectives and provide progress monitoring.



<p>Name _____</p> <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-bottom: 10px;"> <i>Daily Review</i> </div> <ol style="list-style-type: none"> <li>1. Which digit is in the tens place?  <div style="display: flex; align-items: center; margin-top: 10px;"> <div style="border: 1px solid black; padding: 2px 10px; margin-right: 10px;">76</div> <div style="border-bottom: 1px solid black; width: 50px; text-align: center;">(Obj. 1)</div> </div> </li>   <li>2. What number is shown?  <div style="display: flex; align-items: center; margin-top: 10px;"> <div style="border-bottom: 1px solid black; width: 50px; text-align: center;">(Obj. 1)</div> </div> </li>   <li>3. <math display="block">\begin{array}{r} 7 \\ + 2 \\ \hline \end{array}</math>      <math display="block">\begin{array}{r} 6 \\ + 3 \\ \hline \end{array}</math> <div style="display: flex; justify-content: flex-end; margin-top: 10px;"> <div style="border-bottom: 1px solid black; width: 50px; text-align: center;">(Obj. 10)</div> </div> </li>   <li>4. <math display="block">\begin{array}{r} 10 \\ - 2 \\ \hline \end{array}</math>      <math display="block">\begin{array}{r} 8 \\ - 3 \\ \hline \end{array}</math> <div style="display: flex; justify-content: flex-end; margin-top: 10px;"> <div style="border-bottom: 1px solid black; width: 50px; text-align: center;">(Obj. 15)</div> </div> </li>   <li>5. Pedro had 10¢. He spent 2¢. How much does he have left?  <div style="display: flex; justify-content: flex-end; margin-top: 10px;"> <div style="border-bottom: 1px solid black; width: 50px; text-align: center;">(Obj. 15)</div> </div> </li> </ol> <p style="font-size: small; text-align: center;">© Math Teachers Press, Inc. Reproduction is strictly prohibited.</p>	<p>Name _____</p> <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-bottom: 10px;"> <i>Daily Review</i> </div> <ol style="list-style-type: none"> <li>1. <math display="block">\begin{array}{r} 9 \\ + 4 \\ \hline \end{array}</math>      <math display="block">\begin{array}{r} 7 \\ + 9 \\ \hline \end{array}</math> <div style="display: flex; justify-content: flex-end; margin-top: 10px;"> <div style="border-bottom: 1px solid black; width: 50px; text-align: center;">(Obj. 10)</div> </div> </li>   <li>2. Write two subtraction facts for the addition fact <math>7 + 6 = 13</math>.  <div style="display: flex; justify-content: flex-end; margin-top: 10px;"> <div style="border-bottom: 1px solid black; width: 100px; text-align: center;">(Obj. 19)</div> </div> </li>   <li>3. Carlos scored 9 goals last season. Pete scored 7 goals. How many goals were scored in all?  <div style="display: flex; justify-content: flex-end; margin-top: 10px;"> <div style="border-bottom: 1px solid black; width: 50px; text-align: center;">(Obj. 10)</div> </div> </li>   <li>4. Neela baked 12 brownies. She gave 8 brownies away to her friends. How many brownies are left?  <div style="display: flex; justify-content: flex-end; margin-top: 10px;"> <div style="border-bottom: 1px solid black; width: 50px; text-align: center;">(Obj. 15)</div> </div> </li>   <li>5. <math display="block">\begin{array}{r} 6 \\ + 6 \\ \hline \end{array}</math>      <math>7 + 8 = \square</math> <div style="display: flex; justify-content: flex-end; margin-top: 10px;"> <div style="border-bottom: 1px solid black; width: 50px; text-align: center;">(Obj. 10)</div> </div> </li> </ol> <p style="font-size: small; text-align: center;">© Math Teachers Press, Inc. Reproduction is strictly prohibited.</p>
Review 1	Review 2

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## Step 6: Review and Reteach

The Daily Review Record Sheet allows students to track their strengths and weaknesses.

It also suggests *Skill Builder* reteaching pages for missed objectives.



28  
Assessment

### B1 Daily Reviews

Record the results from your Daily Reviews here. The label "Obj.," shows which objective that problem covered.

	Review 1	Review 2	Review 3	Review 4	Review 5	Review 6	Review 7
1	Obj. 1 (SB 1-3)	Obj. 10 (SB 10-2)	Obj. 1 (SB 1-1)	Obj. 1 (SB 1-1)	Obj. 1 (SB 1-1)	Obj. 2 (SB 2-2)	Obj. 3 (SB 3-1)
2	Obj. 1 (SB 1-3)	Obj. 19 (SB 19-3)	Obj. 1 (SB 1-1)	Obj. 1 (SB 1-1)	Obj. 1 (SB 1-1)	Obj. 2 (SB 2-2)	Obj. 3 (SB 3-2)
3	Obj. 10 (SB 10-1)	Obj. 10 (SB 10-2)	Obj. 1 (SB 1-1)	Obj. 2	Obj. 2	Obj. 2	Obj. 3 (SB 3-2)
4	Obj. 15 (SB 15-1)	Obj. 15 (SB 15-2)	Obj. 1 (SB 1-2)	Obj. 2	Obj. 2	Obj. 2	Obj. 8 (SB 48-2)
5	Obj. 15 (SB 15-1)	Obj. 10 (SB 10-1)	Obj. 1 (SB 1-2)	Obj. 2	Obj. 2	Obj. 2	Obj. 8 (SB 48-2)
	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct
	Review 8	Review 9	Review 10	Review 11	Review 12	Review 13	Review 14
1	Obj. 48 (SB 48-3)	Obj. 4 (SB 4-1)	Obj. 6 (SB 6-2)	Obj. 4	Obj. 4	Obj. 4	Obj. 9 (SB 9-1)
2	Obj. 48 (SB 48-3)	Obj. 2 (SB 2-3)	Obj. 6 (SB 6-2)	Obj. 2	Obj. 2	Obj. 2	Obj. 9 (SB 9-2)
3	Obj. 4 (SB 4-1)	Obj. 6 (SB 6-2)	Obj. 5 (SB 5-2)	Obj. 6	Obj. 6	Obj. 6	Obj. 14 (SB 14-1)
4	Obj. 4 (SB 4-1)	Obj. 6 (SB 6-2)	Obj. 4 (SB 4-2)	Obj. 2	Obj. 2	Obj. 2	Obj. 10 (SB 10-3)
5	Obj. 2 (SB 2-3)	Obj. 2 (SB 2-4)	Obj. 7 (SB 7-1)	Obj. 5	Obj. 5	Obj. 5	Obj. 10 (SB 10-4)
	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct
	Review 15	Review 16	Review 17	Review 18	Review 19	Review 20	Review 21
1	Obj. 14 (SB 14-2)	Obj. 10 (SB 10-6)	Obj. 14 (SB 14-2)	Obj. 10	Obj. 10	Obj. 10	Obj. 15 (SB 15-4)
2	Obj. 10 (SB 10-4)	Obj. 10 (SB 10-9)	Obj. 10 (SB 10-3)	Obj. 10	Obj. 10	Obj. 10	Obj. 15 (SB 15-5)
3	Obj. 10 (SB 10-5)	Obj. 10 (SB 10-10)	Obj. 10 (SB 10-5)	Obj. 10	Obj. 10	Obj. 10	Obj. 15 (SB 15-7)
4	Obj. 10 (SB 10-6)	Obj. 10 (SB 10-13)	Obj. 10 (SB 10-6)	Obj. 10	Obj. 10	Obj. 10	Obj. 15 (SB 15-8)
5	Obj. 10 (SB 10-9)	Obj. 10 (SB 10-12)	Obj. 10 (SB 10-9)	Obj. 10	Obj. 10	Obj. 10	Obj. 15 (SB 15-9)
	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct
	Review 22	Review 23	Review 24	Review 25	Review 26	Review 27	Review 28
1	Obj. 15 (SB 15-9)	Obj. 15 (SB 15-4)	Obj. 15 (SB 15-11)	Obj. 15 (SB 15-15)	Obj. 16 (SB 16-1)	Obj. 10 (SB 10-14)	Obj. 10 (SB 10-14)
2	Obj. 15 (SB 15-9)	Obj. 15 (SB 15-5)	Obj. 15 (SB 15-12)	Obj. 15 (SB 15-15)	Obj. 47 (SB 47-2)	Obj. 15 (SB 15-16)	Obj. 47 (SB 47-4)
3	Obj. 15 (SB 15-11)	Obj. 15 (SB 15-7)	Obj. 15 (SB 15-15)	Obj. 16 (SB 16-1)	Obj. 47 (SB 47-3)	Obj. 47 (SB 47-4)	Obj. 15 (SB 15-18)
4	Obj. 15 (SB 15-12)	Obj. 15 (SB 15-8)	Obj. 15 (SB 15-15)	Obj. 47 (SB 47-1)	Obj. 10 (SB 10-14)	Obj. 47 (SB 47-4)	Obj. 15 (SB 15-18)
5	Obj. 15 (SB 15-15)	Obj. 15 (SB 15-9)	Obj. 15 (SB 15-15)	Obj. 47 (SB 47-3)	Obj. 10 (SB 10-14)	Obj. 15 (SB 15-18)	Obj. 15 (SB 15-18)
	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct
	Review 29	Review 30	Review 31	Review 32	Review 33	Review 34	Review 35
1	Obj. 47 (SB 47-3)	Obj. 15 (SB 15-18)	Obj. 50 (SB 50-3)	Obj. 12 (SB 12-1)	Obj. 12 (SB 12-1)	Obj. 12 (SB 12-1)	Obj. 12 (SB 12-1)
2	Obj. 10 (SB 10-14)	Obj. 50 (SB 50-1)	Obj. 50 (SB 50-3)	Obj. 12 (SB 12-2)	Obj. 12 (SB 12-2)	Obj. 12 (SB 12-2)	Obj. 12 (SB 12-2)
3	Obj. 15 (SB 15-16)	Obj. 50 (SB 50-1)	Obj. 12 (SB 12-1)	Obj. 13 (SB 13-1)	Obj. 13 (SB 13-1)	Obj. 13 (SB 13-1)	Obj. 13 (SB 13-1)
4	Obj. 47 (SB 47-4)	Obj. 50 (SB 50-2)	Obj. 12 (SB 12-2)	Obj. 17 (SB 17-1)	Obj. 17 (SB 17-1)	Obj. 17 (SB 17-1)	Obj. 17 (SB 17-1)
5	Obj. 15 (SB 15-18)	Obj. 50 (SB 50-2)	Obj. 12 (SB 12-2)	Obj. 17 (SB 17-2)	Obj. 17 (SB 17-2)	Obj. 17 (SB 17-2)	Obj. 17 (SB 17-2)
	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct

Review 2

Obj. 10 (SB 10-2)

Obj. 19 (SB 19-3)

Obj. 10 (SB 10-2)

Obj. 15 (SB 15-2)

Obj. 10 (SB 10-1)

# Correct

Record results of Daily Reviews by marking a "✓" next to *missed* questions/objectives. Write the **total correct** for each Daily Review in the space provided. For extra practice, use the *Skill Builders* page next to missed/checked objectives.

Ⓢ Denotes Checkpoint Reviews.

Name \_\_\_\_\_

# Moving with Math<sup>®</sup> Learning System

## Step 6: Review and Reteach

*Skill Builders* provide extra practice and homework.

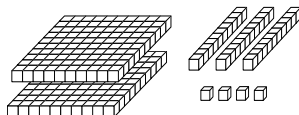


Name \_\_\_\_\_

### Place Value in a 3-Digit Number

Ten of the long blocks or tens will make a flat.  
The flat square block is a model of the 100s or hundreds.

Here is a model of the number 234.

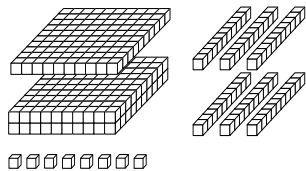


The names of the first three places are shown on this place value mat. Notice that the value of any digit depends upon its place on this mat.

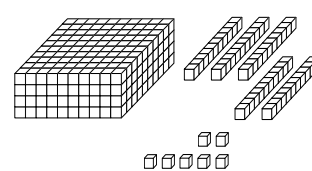
hundreds	tens	ones
2	3	4

Write the number that matches each model.

1. \_\_\_\_\_



2. \_\_\_\_\_



3. **235**

Which digit is in the ones place? \_\_\_\_\_  
Which digit is in the tens place? \_\_\_\_\_  
Which digit is in the hundreds place? \_\_\_\_\_

4. **538**

Which digit is in the ones place? \_\_\_\_\_  
The tens place? \_\_\_\_\_  
The hundreds place? \_\_\_\_\_

5. **307**

Which digit is in the ones place? \_\_\_\_\_  
The tens place? \_\_\_\_\_  
The hundreds place? \_\_\_\_\_

6. **952**

Which digit is in the tens place? \_\_\_\_\_  
The ones place? \_\_\_\_\_  
The hundreds place? \_\_\_\_\_

7. **600**

Which digit is in the ones place? \_\_\_\_\_  
The tens place? \_\_\_\_\_  
The hundreds place? \_\_\_\_\_

8. **349**

Which digit is in the hundreds place? \_\_\_\_\_  
The ones place? \_\_\_\_\_  
The tens place? \_\_\_\_\_

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## Step 7: Reassess with Post-Test



Name \_\_\_\_\_

Score \_\_\_\_\_

(50 possible)

### Number Sense, Addition, Subtraction Post-Test

1. Which digit is in the hundreds place?

7 2 4

(Obj. 1)

- A 7  
B 0  
C 2  
D 4

2. What is the standard numeral for  $400 + 60 + 9$ ?

- A 400,609  
B 40,609  
C 4069  
D 469

(Obj. 1)

3. Which number is greatest?

- A 3462  
B 3612  
C 4321  
D 4312

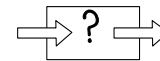
(Obj. 2)

4. Which grade has the most students?

Grade	Number of Students
2	681
3	727
4	679
5	743

- A Grade 2  
B Grade 3  
C Grade 4  
D Grade 5

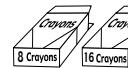
5. A number machine makes numbers in a pattern. What number will come next?



4, 8, 12, \_\_\_\_\_

- A 13  
B 14  
C 15  
D 16

6. An even number of crayons to be packed in a box is not possible.



A B C D

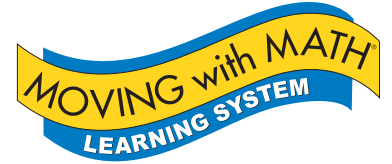
**Record Post-Test Results on Class Record Sheet and Student Progress Report**



# Moving with Math<sup>®</sup> Learning System

## Curriculum Alignment

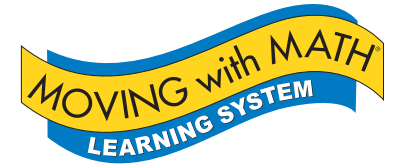
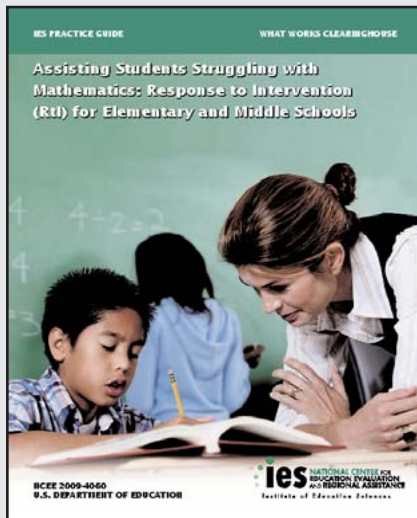
A system of assessment and instruction where everything is tied to objectives and standards..with proven results!



# Meeting Your Needs for RTI

## What Works Clearinghouse Practice Guide

### *Assisting Students Struggling with Mathematics: Response to Intervention (RtI) for Elementary and Middle School*



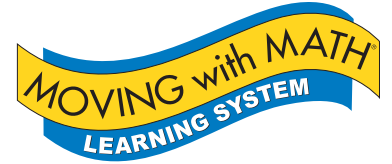
## Summary of Best Practices

- Screen all students to identify those at risk
- In-depth instruction of whole numbers through grade 5 and rational numbers in grades 4-8
- Explicit and systematic instruction
- Instruction on solving word problems
- Physical and visual representations of mathematical ideas
- Building fluent retrieval of basic facts
- Progress monitoring
- Motivational strategies

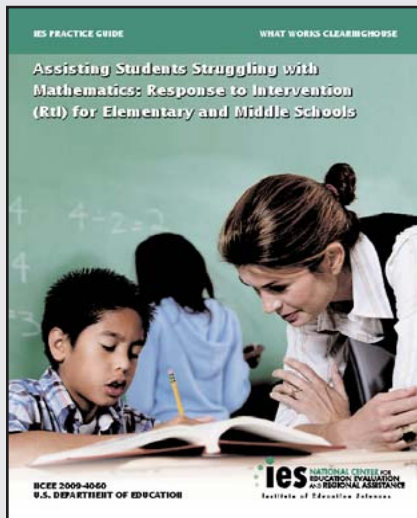


# Meeting Your Needs for RTI

## What Works Clearinghouse Practice Guide

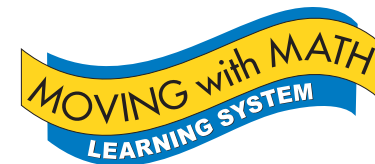


## 2. In-Depth Instruction of Whole Numbers through Grade 5 and Rational Numbers in Grades 4-8



# Meeting Your Needs for RTI

## What Works Clearinghouse Practice Guide



### 3. Explicit and Systematic Instruction

#### Objective:

To explore and name base ten blocks. To match the blocks with their place value names.

#### Materials:

Base ten blocks, Place Value Mats (Masters 1 and 2)

*Note: Before class, make copies of Master 20 (Vocabulary Cards). Make copies of Master 21 (My Math Glossary) and distribute to each student.*

#### Vocabulary:

different, place value names, same



*One Hundred Is a Family*, Ryan, Pam Munoz (Activity 2)

#### Introductory Activities

##### Introducing Base Ten Blocks

The main reason students make errors with whole number algorithms is that they do not understand multidigit numeration. They do not know that 43 means 4 tens and 3 ones or  $40 + 3$ .

Base ten blocks are ideal for teaching numeration concepts because students can see the abstract concept of place value each time they pick up a block. One tens block is always seen both as 1 ten and 10 ones.

Each pair or small group should have 20 ones blocks, 10 tens blocks, 10 hundreds blocks, and a place value mat.

Explain the benefits and proper use of manipulatives. Set ground rules for using them and discuss take-out and clean-up routines.

**We are going to begin using base ten blocks. See what you can discover about your blocks.** Allow exploratory time. Students might make buildings, roads and parking ramps.

Encourage students to look for patterns. **We can find important patterns if we ask ourselves how these blocks are the same, or alike, and how they are different, or not alike.**

Write 2 columns on the board:

How are the blocks the same?  
How are the blocks different?

**What is one way the blocks are the same?** (e.g., same material) After a period of time, ask students to share.

Same	Different
made of wood	sizes
natural color	shapes
points & corners	volumes
solids	weight
made of 1 cm cubes	
10 of 1 block = 1 of the next larger block	

**How many different sizes do you have? (3) Put 1 of each size in front of you. We call the smallest block the “ones” or “units” block. How many ones does it take to make the next-sized block? (10) We name this block the “tens” or “long” block.**

**How many of the ones blocks are the same as the largest block? (100) We name this block the “hundreds” or “flat” block.**

The words “ones,” “tens,” and “hundreds” are **place value names**.

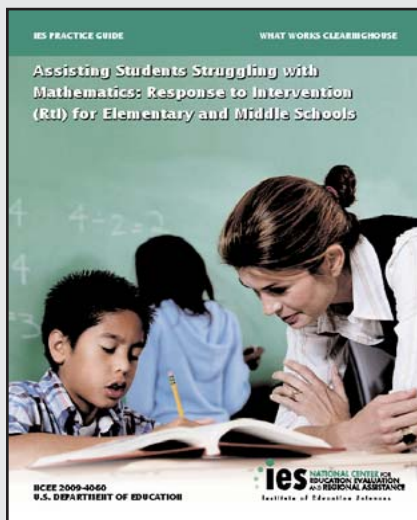
Display 1 hundred, 2 tens, 5 ones. Place the blocks correctly on a Place Value Mat. Then say the words for the blocks, **one hundred twenty-five**.

#### About This Page

Work through the example together. **Look at problem 1. What blocks are shown?** (1 hundred, 5 tens, 3 ones) **Write the number in the correct place on the chart.** (153)

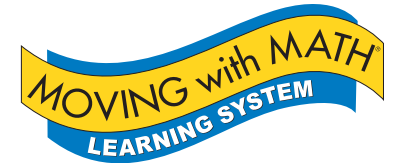
**To say this number aloud, touch the biggest block and say its value.** (100) **Now touch the next biggest blocks and say their value.** (50) **Then touch the smallest blocks and say their value.** (3) **Now say the number together as you touch the blocks.** (one hundred fifty-three)

Have students complete problems 2 and 3 on their own or with a partner.



# Meeting Your Needs for RTI

## What Works Clearinghouse Practice Guide



# 4. Instruction on Solving Word Problems

**Objective:**  
To solve word problems using the clue word “in all.”

**Materials:**  
Five Steps in Problem Solving (from Master 13), chart paper or tagboard

**Vocabulary:**  
variable

### Introductory Activities

**n=? Problem Solving Steps**  
During this activity, the teacher may start a chart of problem-solving steps for the class if desired. Students may also be given a copy of Master 13 as a reference.

Write on the board:  
Wayne has 36 baseball cards. Terry has 48 baseball cards. How many cards do they have in all?

**We are going to list the steps you use to solve word problems. What is the first thing you must do? (Read the problem.) You must read the problem and be sure you understand it. A good way to understand a problem is to retell the problem in your own words. Ask a volunteer to read the story aloud. Then have students take turns retelling the story to a partner.**

Write on the chart:

1. Read and understand.  
**What is the next thing you must do?** (Find the question. Find the facts.)
2. Find the question and needed facts.  
Ask a student to identify and underline the question and identify and circle the needed facts.  
Wayne has 36 baseball cards. Terry has 48 baseball cards. How many cards do they have in all?

Is each circled fact related to the question? (yes) If you find a fact that is not related, cross it out.  
**What is this problem about, putting things together or taking things apart?** (putting things together) Help students write a number sentence for their problem.  
 $36 + 48 = \square$

We can use a variable to represent our unknown number. A *variable* is a symbol such as a box or letter used to stand for a number. Have students solve for the unknown number.  
Repeat the activity with a second real-world problem if needed.

**Strategies: Write a Number Sentence**  
You can write a number sentence to help you solve word problems. Represent the unknown number with a shape or letter.

The peanut vendor sold 44 bags of peanuts at one circus and 27 bags of the next circus. How many bags did he sell in all?

$44 + 27 = \square$   
 $44 + 27 = n$   
 $44 + 27 = n$

Underline the clue words. Write a number sentence. Solve the problem.

1. The circus lions ate 39 pounds of meat on Monday and 58 pounds of meat on Tuesday. How much meat did the lions eat in all?  
 $39 + 56 = \square$   
 $\square = 95$  pounds
2. Lawrence, the circus strong lady, can hold 25 rubber balls in one hand and 38 balls in the other. How many balls can she hold in all?  
 $25 + 36 = \triangle$   
 $\triangle = 61$  balls
3. Linda's teacher asked her to do 55 addition problems and 38 subtraction problems. How many math problems did the teacher assign in all?  
 $56 + 26 = \square$   
 $\square = 81$  problems
4. On a trip to Canada, Dad drove 412 miles and Mom drove 402 miles. How many miles did they drive altogether?  
 $465 + 412 = \square$   
 $\square = 877$  miles
5. On Thursday, 370 students went out for the play. On Friday, 467 more did.  
 $370 + 147 = \square$   
 $\square = 517$  students
6. The car wash used 422 gallons of water to wash trucks. Another 203 gallons were used to wash cars. How many gallons were used altogether?  
 $422 + 263 = \square$   
 $\square = 685$

### About This Page

Together, read the example at the top of the page. Discuss the clue words “in all.” Have students do the rest of the page on their own or with a partner.

### Follow Up Activities

Give students examples of addition word problems having too much information in them, pointing out that sometimes you don't need to use all the information in a problem.  
**Example:** Jane is 10 years old and weighs 70 pounds. Alex is 9 years old and weighs 60 pounds. How much would a scale show if they stood on it together?

### SKILL BUILDERS 10-13

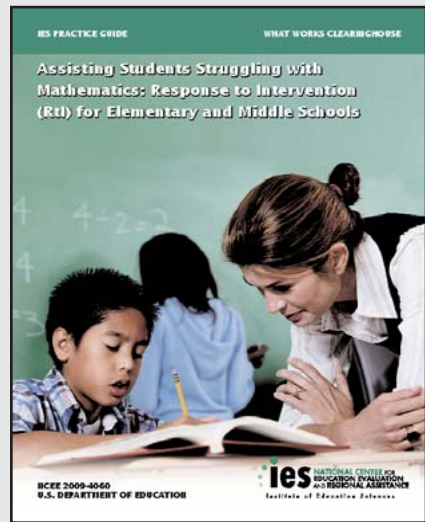
### Five Steps in Problem Solving

- Step 1. Read and understand.
- Step 2. Find the question and needed facts.
- Step 3. Decide on a process.
- Step 4. Estimate.
- Step 5. Solve and check back.

### Problem-Solving Strategies

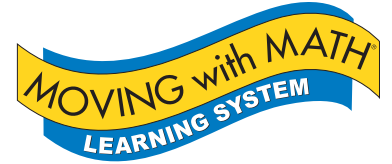
1. Act it out.
2. Use a model.
3. Draw a picture.
4. Simplify.
5. Make a table.
6. Guess and check.
7. Write a number sentence.

Master 13  
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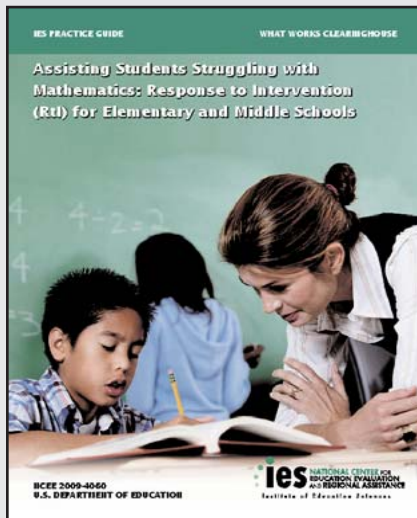


# Meeting Your Needs for RTI

## What Works Clearinghouse Practice Guide

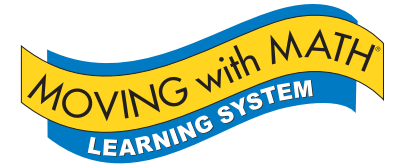


# 5. Physical and Visual Representations of Mathematical Ideas



# Meeting Your Needs for RTI

## What Works Clearinghouse Practice Guide



# 6. Building Fluent Retrieval of Basic Facts

### Subtraction Facts

100 Basic Subtraction Facts

$\begin{array}{r} 7 \\ -1 \end{array}$	$\begin{array}{r} 13 \\ -6 \end{array}$	$\begin{array}{r} 9 \\ -4 \end{array}$	$\begin{array}{r} 16 \\ -7 \end{array}$	$\begin{array}{r} 6 \\ -6 \end{array}$	$\begin{array}{r} 12 \\ -4 \end{array}$	$\begin{array}{r} 7 \\ -7 \end{array}$	$\begin{array}{r} 4 \\ -1 \end{array}$
$\begin{array}{r} 11 \\ -7 \end{array}$	$\begin{array}{r} 6 \\ -0 \end{array}$	$\begin{array}{r} 8 \\ -4 \end{array}$	$\begin{array}{r} 4 \\ -3 \end{array}$	$\begin{array}{r} 10 \\ -6 \end{array}$	$\begin{array}{r} 16 \\ -9 \end{array}$	$\begin{array}{r} 7 \\ -6 \end{array}$	$\begin{array}{r} 6 \\ -5 \end{array}$
$\begin{array}{r} 6 \\ -3 \end{array}$	$\begin{array}{r} 14 \\ -9 \end{array}$	$\begin{array}{r} 9 \\ -9 \end{array}$	$\begin{array}{r} 7 \\ -2 \end{array}$	$\begin{array}{r} 17 \\ -8 \end{array}$	$\begin{array}{r} 2 \\ -1 \end{array}$	$\begin{array}{r} 4 \\ -2 \end{array}$	$\begin{array}{r} 14 \\ -5 \end{array}$
$\begin{array}{r} 6 \\ -2 \end{array}$	$\begin{array}{r} 15 \\ -7 \end{array}$	$\begin{array}{r} 3 \\ -2 \end{array}$	$\begin{array}{r} 8 \\ -5 \end{array}$	$\begin{array}{r} 15 \\ -8 \end{array}$	$\begin{array}{r} 7 \\ -5 \end{array}$	$\begin{array}{r} 8 \\ -1 \end{array}$	$\begin{array}{r} 13 \\ -8 \end{array}$
$\begin{array}{r} 12 \\ -8 \end{array}$	$\begin{array}{r} 10 \\ -9 \end{array}$	$\begin{array}{r} 10 \\ -4 \end{array}$	$\begin{array}{r} 10 \\ -1 \end{array}$	$\begin{array}{r} 12 \\ -5 \end{array}$	$\begin{array}{r} 3 \\ -2 \end{array}$	$\begin{array}{r} 10 \\ -5 \end{array}$	$\begin{array}{r} 16 \\ -8 \end{array}$
$\begin{array}{r} 9 \\ -6 \end{array}$	$\begin{array}{r} 1 \\ -0 \end{array}$	$\begin{array}{r} 0 \\ -0 \end{array}$	$\begin{array}{r} 9 \\ -1 \end{array}$	$\begin{array}{r} 15 \\ -9 \end{array}$	$\begin{array}{r} 11 \\ -8 \end{array}$	$\begin{array}{r} 13 \\ -5 \end{array}$	$\begin{array}{r} 11 \\ -6 \end{array}$
$\begin{array}{r} 5 \\ -3 \end{array}$	$\begin{array}{r} 8 \\ -0 \end{array}$	$\begin{array}{r} 13 \\ -7 \end{array}$	$\begin{array}{r} 4 \\ -4 \end{array}$	$\begin{array}{r} 7 \\ -0 \end{array}$	$\begin{array}{r} 2 \\ -0 \end{array}$	$\begin{array}{r} 8 \\ -7 \end{array}$	$\begin{array}{r} 3 \\ -0 \end{array}$
$\begin{array}{r} 8 \\ -6 \end{array}$	$\begin{array}{r} 12 \\ -7 \end{array}$	$\begin{array}{r} 10 \\ -3 \end{array}$	$\begin{array}{r} 14 \\ -6 \end{array}$	$\begin{array}{r} 12 \\ -6 \end{array}$	$\begin{array}{r} 9 \\ -0 \end{array}$	$\begin{array}{r} 9 \\ -7 \end{array}$	$\begin{array}{r} 5 \\ -4 \end{array}$
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Master 17

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### Addition Facts

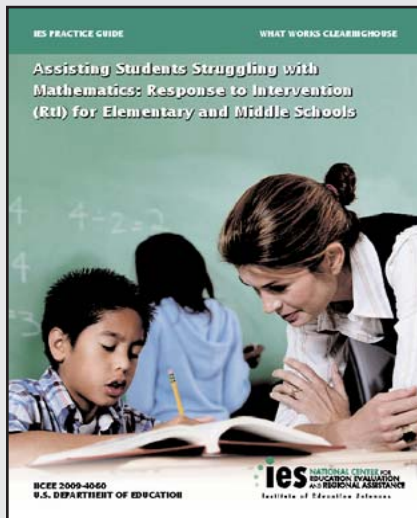
100 Basic Addition Facts

Score \_\_\_\_\_

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$\begin{array}{r} 1 \\ +7 \end{array}$	$\begin{array}{r} 7 \\ +6 \end{array}$	$\begin{array}{r} 4 \\ +3 \end{array}$	$\begin{array}{r} 5 \\ +8 \end{array}$	$\begin{array}{r} 8 \\ +2 \end{array}$	$\begin{array}{r} 6 \\ +4 \end{array}$	$\begin{array}{r} 0 \\ +5 \end{array}$	$\begin{array}{r} 9 \\ +9 \end{array}$	$\begin{array}{r} 2 \\ +0 \end{array}$	$\begin{array}{r} 3 \\ +1 \end{array}$
$\begin{array}{r} 0 \\ +2 \end{array}$	$\begin{array}{r} 2 \\ +9 \end{array}$	$\begin{array}{r} 7 \\ +7 \end{array}$	$\begin{array}{r} 9 \\ +3 \end{array}$	$\begin{array}{r} 4 \\ +0 \end{array}$	$\begin{array}{r} 3 \\ +5 \end{array}$	$\begin{array}{r} 6 \\ +8 \end{array}$	$\begin{array}{r} 5 \\ +6 \end{array}$	$\begin{array}{r} 1 \\ +1 \end{array}$	$\begin{array}{r} 8 \\ +4 \end{array}$
$\begin{array}{r} 4 \\ +8 \end{array}$	$\begin{array}{r} 8 \\ +7 \end{array}$	$\begin{array}{r} 6 \\ +9 \end{array}$	$\begin{array}{r} 7 \\ +0 \end{array}$	$\begin{array}{r} 9 \\ +5 \end{array}$	$\begin{array}{r} 5 \\ +1 \end{array}$	$\begin{array}{r} 0 \\ +4 \end{array}$	$\begin{array}{r} 1 \\ +3 \end{array}$	$\begin{array}{r} 3 \\ +6 \end{array}$	$\begin{array}{r} 2 \\ +2 \end{array}$
$\begin{array}{r} 7 \\ +4 \end{array}$	$\begin{array}{r} 3 \\ +3 \end{array}$	$\begin{array}{r} 2 \\ +1 \end{array}$	$\begin{array}{r} 8 \\ +9 \end{array}$	$\begin{array}{r} 6 \\ +0 \end{array}$	$\begin{array}{r} 9 \\ +8 \end{array}$	$\begin{array}{r} 1 \\ +6 \end{array}$	$\begin{array}{r} 4 \\ +5 \end{array}$	$\begin{array}{r} 0 \\ +7 \end{array}$	$\begin{array}{r} 5 \\ +2 \end{array}$
$\begin{array}{r} 6 \\ +1 \end{array}$	$\begin{array}{r} 2 \\ +4 \end{array}$	$\begin{array}{r} 0 \\ +6 \end{array}$	$\begin{array}{r} 3 \\ +2 \end{array}$	$\begin{array}{r} 7 \\ +3 \end{array}$	$\begin{array}{r} 9 \\ +7 \end{array}$	$\begin{array}{r} 5 \\ +0 \end{array}$	$\begin{array}{r} 8 \\ +8 \end{array}$	$\begin{array}{r} 4 \\ +9 \end{array}$	$\begin{array}{r} 1 \\ +5 \end{array}$
$\begin{array}{r} 5 \\ +4 \end{array}$	$\begin{array}{r} 7 \\ +2 \end{array}$	$\begin{array}{r} 6 \\ +5 \end{array}$	$\begin{array}{r} 1 \\ +9 \end{array}$	$\begin{array}{r} 0 \\ +1 \end{array}$	$\begin{array}{r} 8 \\ +3 \end{array}$	$\begin{array}{r} 2 \\ +8 \end{array}$	$\begin{array}{r} 3 \\ +7 \end{array}$	$\begin{array}{r} 9 \\ +0 \end{array}$	$\begin{array}{r} 4 \\ +6 \end{array}$
$\begin{array}{r} 8 \\ +6 \end{array}$	$\begin{array}{r} 3 \\ +9 \end{array}$	$\begin{array}{r} 9 \\ +4 \end{array}$	$\begin{array}{r} 6 \\ +2 \end{array}$	$\begin{array}{r} 5 \\ +5 \end{array}$	$\begin{array}{r} 1 \\ +0 \end{array}$	$\begin{array}{r} 0 \\ +3 \end{array}$	$\begin{array}{r} 1 \\ +1 \end{array}$	$\begin{array}{r} 7 \\ +8 \end{array}$	$\begin{array}{r} 2 \\ +7 \end{array}$
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Master 15

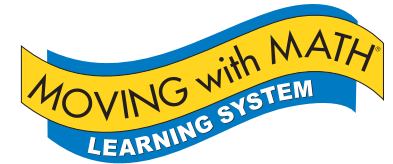
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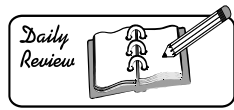
# Meeting Your Needs for RTI

## What Works Clearinghouse Practice Guide



# 7. Progress Monitoring

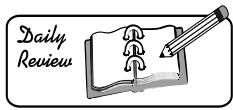
Name \_\_\_\_\_



1. Which digit is in the tens place?

76

 (Obj. 1)



1. 
$$\begin{array}{r} 9 \quad 7 \\ + 4 \quad + 9 \\ \hline \end{array}$$
 (Obj. 10)

2. What

3. 
$$\begin{array}{r} 7 \\ + 2 \\ \hline \end{array}$$

4. 
$$\begin{array}{r} 10 \\ - 2 \\ \hline \end{array}$$

5. Pedro How

28 Assessment

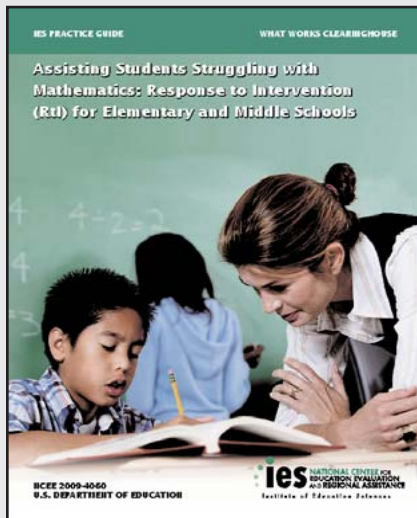
**B1 Daily Reviews** Record the results from your Daily Reviews here. The label "Obj." shows which objective that problem covered.

	Review 1	Review 2	Review 3	Review 4	Review 5	Review 6	Review 7	
1	Obj. 1 (SB 1-3)	Obj. 10 (SB 10-2)	Obj. 1 (SB 1-1)	Obj. 1 (SB 1-1)	Obj. 1 (SB 1-1)	Obj. 2 (SB 2-2)	Obj. 3 (SB 3-1)	
2	Obj. 1 (SB 1-3)	Obj. 19 (SB 19-3)	Obj. 1 (SB 1-1)	Obj. 1 (SB 1-2)	Obj. 1 (SB 1-1)	Obj. 2 (SB 2-2)	Obj. 3 (SB 3-2)	
3	Obj. 10 (SB 10-1)	Obj. 10 (SB 10-2)	Obj. 1 (SB 1-1)	Obj. 2 (SB 2-1)	Obj. 1 (SB 1-2)	Obj. 3 (SB 3-1)	Obj. 3 (SB 3-2)	
4	Obj. 15 (SB 15-1)	Obj. 15 (SB 15-2)	Obj. 1 (SB 1-2)	Obj. 2 (SB 2-2)	Obj. 1 (SB 1-1)	Obj. 3 (SB 3-2)	Obj. 48 (SB 48-2)	
5	Obj. 15 (SB 15-1)	Obj. 10 (SB 10-1)	Obj. 1 (SB 1-2)	Obj. 2 (SB 2-2)	Obj. 2 (SB 2-1)	Obj. 3 (SB 3-2)	Obj. 48 (SB 48-2)	
	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	
	Review 8	Review 9	Review 10	Review 11	Review 12	Review 13	Review 14	
1	Obj. 48 (SB 48-3)	Obj. 4 (SB 4-1)	Obj. 6 (SB 6-2)	Obj. 4 (SB 4-1)	Obj. 5 (SB 5-2)	Obj. 7 (SB 7-1)	Obj. 9 (SB 9-1)	
2	Obj. 48 (SB 48-3)	Obj. 2 (SB 2-3)	Obj. 6 (SB 6-2)	Obj. 2 (SB 2-3)	Obj. 4 (SB 4-2)	Obj. 8 (SB 8-2)	Obj. 9 (SB 9-2)	
3	Obj. 4 (SB 4-1)	Obj. 6 (SB 6-2)	Obj. 5 (SB 5-2)	Obj. 6 (SB 6-1)	Obj. 7 (SB 7-1)	Obj. 8 (SB 8-3)	Obj. 14 (SB 14-1)	
4	Obj. 4 (SB 4-1)	Obj. 6 (SB 6-2)	Obj. 4 (SB 4-2)	Obj. 2 (SB 2-4)	Obj. 8 (SB 8-2)	Obj. 9 (SB 9-1)	Obj. 10 (SB 10-3)	
5	Obj. 2 (SB 2-3)	Obj. 2 (SB 2-4)	Obj. 7 (SB 7-1)	Obj. 5 (SB 5-2)	Obj. 8 (SB 8-1)	Obj. 9 (SB 9-2)	Obj. 10 (SB 10-4)	
	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	
	Review 15	Review 16	Review 17	Review 18	Review 19	Review 20	Review 21	
1	Obj. 14 (SB 14-2)	Obj. 10 (SB 10-6)	Obj. 14 (SB 14-2)	Obj. 10 (SB 10-10)	Obj. 15 (SB 15-15)	Obj. 19 (SB 19-2)	Obj. 15 (SB 15-4)	
2	Obj. 10 (SB 10-4)	Obj. 10 (SB 10-9)	Obj. 10 (SB 10-3)	Obj. 10 (SB 10-11)	Obj. 11 (SB 11-1)	Obj. 15 (SB 15-3)	Obj. 15 (SB 15-5)	
3	Obj. 10 (SB 10-5)	Obj. 10 (SB 10-10)	Obj. 10 (SB 10-5)	Obj. 10 (SB 10-12)	Obj. 19 (SB 19-1)	Obj. 15 (SB 15-4)	Obj. 15 (SB 15-7)	
4	Obj. 10 (SB 10-6)	Obj. 10 (SB 10-13)	Obj. 10 (SB 10-6)	Obj. 15 (SB 15-15)	Obj. 15 (SB 15-3)	Obj. 15 (SB 15-5)	Obj. 15 (SB 15-8)	
5	Obj. 10 (SB 10-9)	Obj. 10 (SB 10-12)	Obj. 10 (SB 10-9)	Obj. 11 (SB 11-1)	Obj. 15 (SB 15-3)	Obj. 15 (SB 15-6)	Obj. 15 (SB 15-9)	
	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	
	Review 22	Review 23	Review 24	Review 25	Review 26	Review 27	Review 28	
1	Obj. 15 (SB 15-9)	Obj. 15 (SB 15-4)	Obj. 15 (SB 15-11)	Obj. 15 (SB 15-15)	Obj. 16 (SB 16-1)	Obj. 10 (SB 10-14)	Obj. 10 (SB 10-14)	
2	Obj. 15 (SB 15-9)	Obj. 15 (SB 15-5)	Obj. 15 (SB 15-12)	Obj. 15 (SB 15-15)	Obj. 47 (SB 47-2)	Obj. 15 (SB 15-16)	Obj. 47 (SB 47-4)	
3	Obj. 15 (SB 15-11)	Obj. 15 (SB 15-7)	Obj. 15 (SB 15-15)	Obj. 16 (SB 16-1)	Obj. 47 (SB 47-3)	Obj. 47 (SB 47-4)	Obj. 15 (SB 15-18)	
4	Obj. 15 (SB 15-12)	Obj. 15 (SB 15-8)	Obj. 15 (SB 15-15)	Obj. 47 (SB 47-1)	Obj. 10 (SB 10-14)	Obj. 47 (SB 47-4)	Obj. 15 (SB 15-18)	
5	Obj. 15 (SB 15-15)	Obj. 15 (SB 15-9)	Obj. 15 (SB 15-15)	Obj. 47 (SB 47-3)	Obj. 10 (SB 10-14)	Obj. 15 (SB 15-18)	Obj. 15 (SB 15-18)	
	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	# Correct	
	Review 29	Review 30	Review 31	Review 32				
1	Obj. 47 (SB 47-3)	Obj. 15 (SB 15-18)	Obj. 50 (SB 50-3)	Obj. 12 (SB 12-1)				
2	Obj. 10 (SB 10-14)	Obj. 50 (SB 50-1)	Obj. 50 (SB 50-3)	Obj. 12 (SB 12-2)				
3	Obj. 15 (SB 15-16)	Obj. 50 (SB 50-1)	Obj. 12 (SB 12-1)	Obj. 13 (SB 13-1)				
4	Obj. 47 (SB 47-4)	Obj. 50 (SB 50-2)	Obj. 12 (SB 12-2)	Obj. 17 (SB 17-1)				
5	Obj. 15 (SB 15-18)	Obj. 50 (SB 50-2)	Obj. 12 (SB 12-2)	Obj. 17 (SB 17-2)				
	# Correct	# Correct	# Correct	# Correct				

Record results of Daily Reviews by marking a "✓" next to missed questions/objectives. Write the total correct for each Daily Review in the space provided. For extra practice, use the *Skill Builders* page next to missed/checked objectives.

Denotes Checkpoint Reviews.

Name \_\_\_\_\_



IES PRACTICE GUIDE WHAT WORKS CLEARINGHOUSE

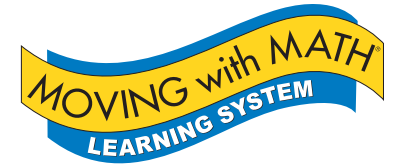
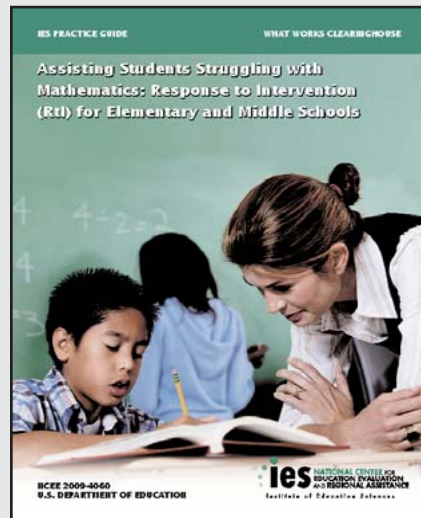
Assisting Students Struggling with Mathematics: Response to Intervention (RTI) for Elementary and Middle Schools

IESCE 2009-4060 U.S. DEPARTMENT OF EDUCATION

ies NATIONAL CENTER FOR EDUCATIONAL EVALUATION AND REGIONAL ASSISTANCE Institute of Education Sciences

# Meeting Your Needs for RTI

## What Works Clearinghouse Practice Guide



## 8. Motivational Strategies

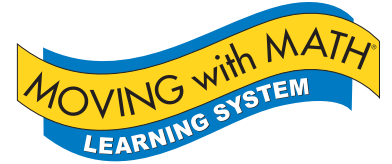


Lesson Plans are guided to provide successful, engaging, and educational experiences

# Meeting Your Needs for RTI

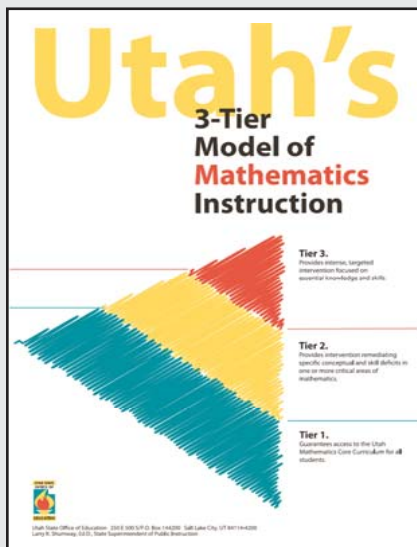
## Utah's 3-Tier Model of Mathematics Instruction

Page 9



## Tier 1 Essential Elements of Instruction

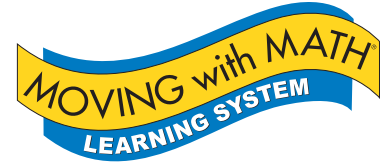
- Differentiated instruction for conceptual development, skill acquisition, and application, including reteaching, and/or additional practice
- Guided practice
- Use of physical, visual, and abstract representations
- Manipulatives as instructional tools



# Meeting Your Needs for RTI

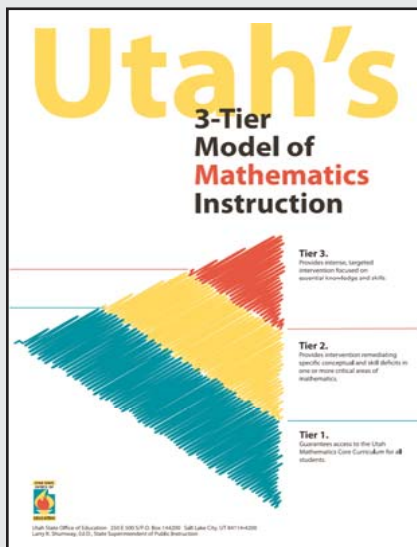
## Utah's 3-Tier Model of Mathematics Instruction

Page 10



## Tier 2 Essential Elements of Instruction

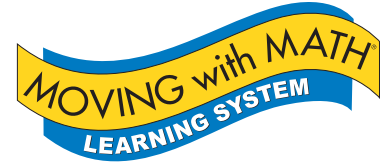
- Targeted, systematic, explicit instruction
- Differentiated instruction in small groups
- Explicit connections between physical, visual, and abstract representations
- Additional conceptual development of core mathematics ideas and skills
- Guided practice to develop skills for independent practice
- Manipulatives for instruction and individual skill practice



# Meeting Your Needs for RTI

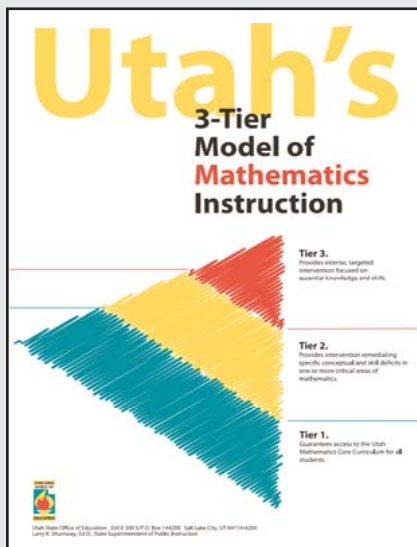
## Utah's 3-Tier Model of Mathematics Instruction

Page 11

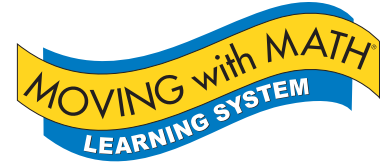


## Tier3 Essential Elements of Instruction

- Explicit, intense, targeted instruction on specific conceptual components for individuals or small groups
- Use of manipulatives for accommodations, conceptual development, and individualized skill practice
- Guided practice to develop specific skills and strategies
- Instructional methods that explicitly link concepts and skills with physical, visual, and abstract representations



# Research Based Strategies and Results

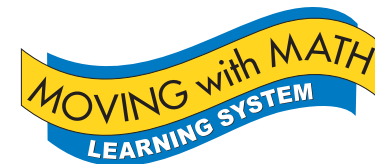


## Research-Based Strategies for Special Education and ELL

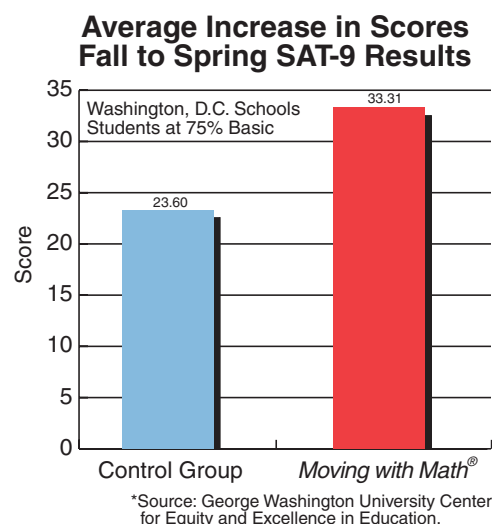
- Include assessment tools to correctly place all learners
- Use manipulatives, pictures, and charts
- Implement scaffolding and front loading
- Introduce new vocabulary words at the beginning of the lesson and develop a glossary
- Use a consistent five-step problem solving plan and strategies
- Encourage peer communication and practice playing games
- Integrate oral and written communication between teacher and students



# Research Based Strategies and Results



## Scientifically Based Research Proves Student Gains

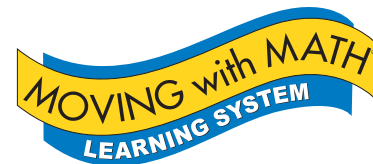


### GWU Study Results

An independent study done by George Washington University found that over 11,000 students in Washington D.C. made statistically significant achievement gains on the SAT-9 compared to a control group in only 30 lessons.

**Basic** and **Below Basic** students made the greatest gains!

The RTI Solution  
for Utah's  
School Districts



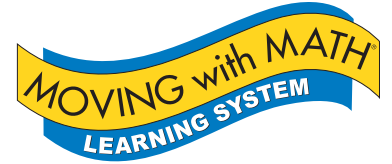
# *Moving with Math*<sup>®</sup> for Utah's School Districts



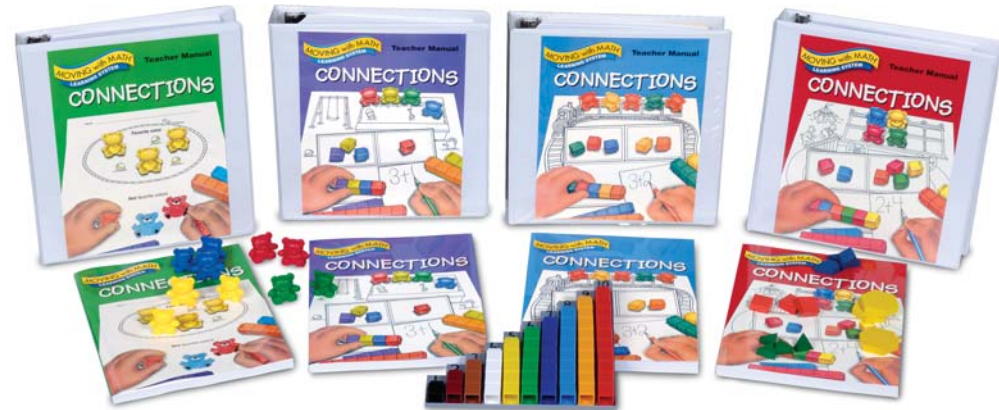


# The Solution

PRE-KINDERGARTEN  
through  
GRADE 2



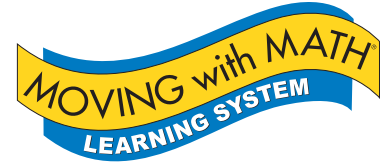
## Connections Pre-Kindergarten through Grade 2



- Cross-curricular approach
- Connections to literacy
- Language acquisition
- Available in Spanish

# The Solution

GRADES 1-4



## Foundations by Topic Grades 1 through 4



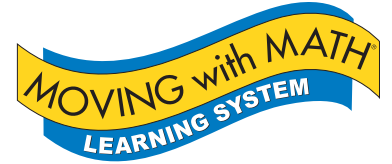
**Level A**  
**(Grades 1 and 2)**

**Level B**  
**(Grades 3 and 4)**

- Comprehensive or targeted intervention
- Connections to literacy
- Spanish/ELL Components

# The Solution

GRADES 5–8



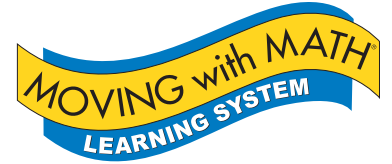
## Math by Topic IM Grades 5 through 8



- Comprehensive or targeted intervention
- Algebra readiness
- Web-based assessment technology available

# The Solution

GRADES 1–8



## Math by Topic Grades 1 through 8

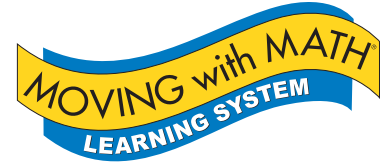


- Comprehensive or targeted intervention
- Reading comprehension level is two grade levels below the math level—great for Tier 3!
- Web-based assessment technology available

# The Solution

GRADES K-8

Condensed  
Intervention  
and/or  
Summer School



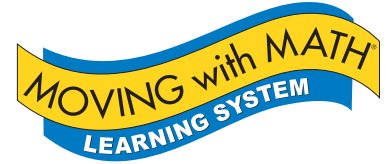
## Extensions Grades K through 8



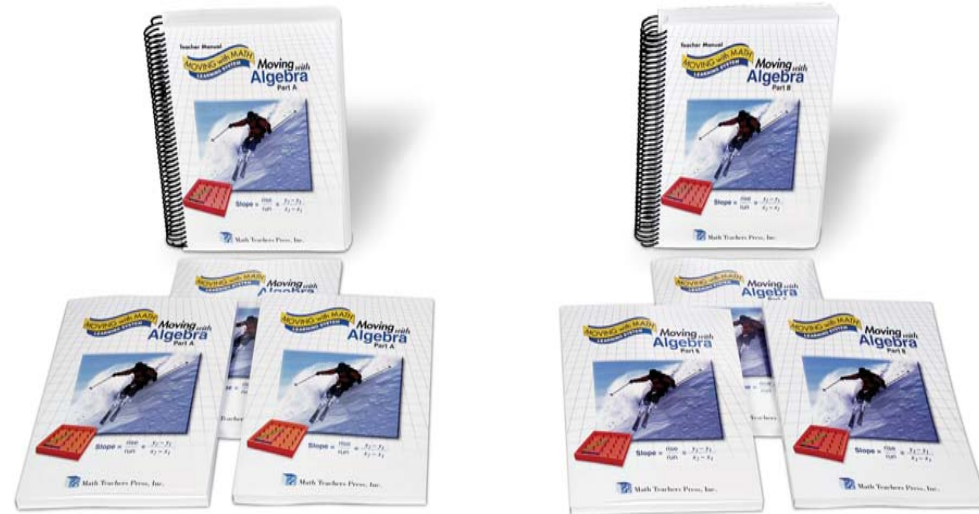
- Condensed math intervention by grade level
- 20 lessons per grade level
- Web-based assessment available

# The Solution

GRADES 7+



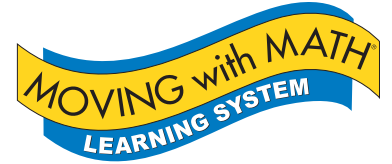
## Moving with Algebra Grades 7 or above



- Pre-algebra/core program
- Double dose/second math class
- Algebra readiness

# The Solution

GRADES 9+



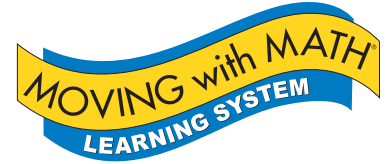
## SUMS (Success Using Math Standards) Grades 9 or above



- Core program
- Double dose/second math class
- Exit exam preparation
- Individualized study program
- Web-based assessment available

# The Solution

## PROFESSIONAL DEVELOPMENT



# Professional Development Implementation Workshop



- Organization of materials
- How to use assessment data to drive instruction
- What to expect the first two days of class
- RTI strategies and best practices



# Contact Me for a Free Webinar

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**P: 800-852-2435**

**“What you have been obliged to discover by yourself leaves a path in your mind which you can use again when the need arises.”**

**-G.C. Lichtenberg**

